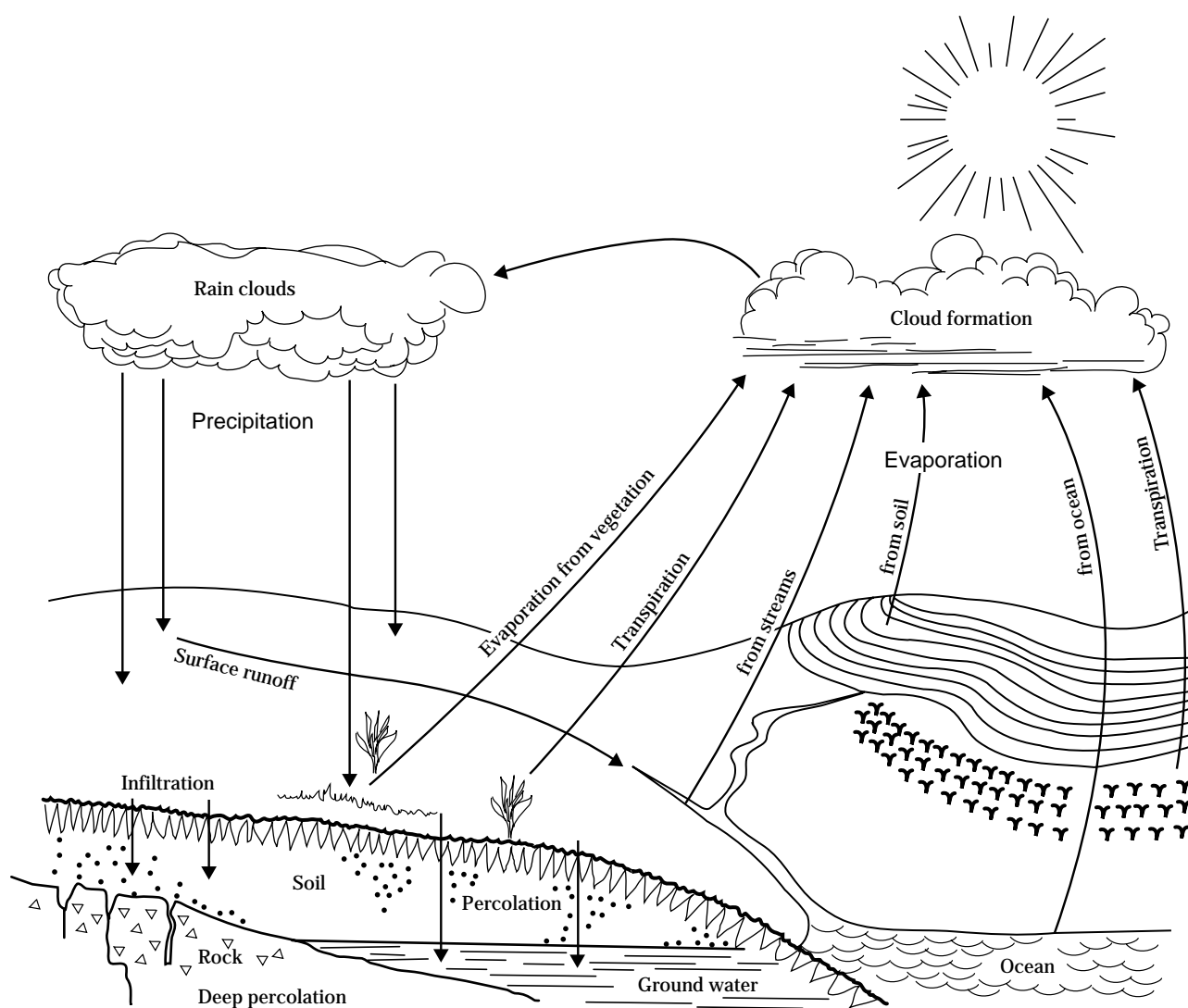


## Chapter 5 Streamflow Data



---

Issued September 1997

The United States Department of Agriculture (USDA) prohibits discrimination in its programs on the basis of race, color, national origin, sex, religion, age, disability, political beliefs, and marital or familial status. (Not all prohibited bases apply to all programs.) Persons with disabilities who require alternative means for communication of program information (Braille, large print, audiotape, etc.) should contact USDA's TARGET Center at (202) 720-2600 (voice and TDD).

To file a complaint, write the Secretary of Agriculture, U.S. Department of Agriculture, Washington, DC 20250, or call 1-800-245-6340 (voice) or (202) 720-1127 (TDD). USDA is an equal employment opportunity employer.

---

# Acknowledgments

---

Chapter 5, Streamflow Data, was originally prepared by **Victor Mockus** (retired) and was reprinted with minor revisions in 1969. This version was prepared by an Agricultural Research Service/Natural Resources Conservation Service (NRCS) workgroup under the guidance of **Norman Miller** (retired), Natural Resources Conservation Service (NRCS), Washington, DC. The workgroup members include **Donald E. Woodward**, national hydraulic engineer, NRCS, Washington, DC, and **William J. Gburek**, hydraulic engineer, Agricultural Research Service (ARS), University Park, PA, co-chairmen; **Allen T. Hjelmfelt, Jr.**, hydraulic engineer, ARS, Columbia, MO; **Robert O. Kluth**, (retired); **Arlis Plummer**, hydraulic engineer, NRCS, Lincoln, NE; **Joe Van Mullen**, hydraulic engineer, NRCS, Bozeman, MT; and **James Hailey**, NRCS, Temple, TX.

Many others including **Gary Conaway**, hydraulic engineer, NRCS, Portland, OR; **Paul Welle**, conservation engineer, NRCS, Beltsville, MD; and **William Merkel**, hydraulic engineer, NRCS, Beltsville, MD, provided comments on the chapter. **Helen Fox Moody**, hydraulic engineer, NRCS, Washington, DC, helped to prepare the final materials, and the Technical Publishing Team, NRCS, Fort Worth, TX, prepared the document for publication.



---

# Chapter 5

# Streamflow Data

---

---

<b>Contents:</b>	<b>630.0500</b>	<b>Introduction</b>	<b>5-1</b>
	<b>630.0501</b>	<b>Sources</b>	<b>5-1</b>
	<b>630.0502</b>	<b>Installation and operation of streamflow stations</b>	<b>5-2</b>
		(a) Temporary streamflow station installations .....	5-2
	<b>630.0503</b>	<b>Streamflow data uses</b>	<b>5-3</b>
		(a) Mean daily discharges .....	5-3
		(b) Transposition of streamflow records .....	5-8
		(c) Volume-duration-probability analysis .....	5-10
		(d) Flow duration curves .....	5-10
		(e) Determination of runoff curve numbers .....	5-10
	<b>630.0504</b>	<b>References</b>	<b>5-15</b>

---

---

<b>Tables</b>	<b>Table 5-1</b>	Mean daily discharges, annual flood period	5-7
	<b>Table 5-2</b>	Factors affecting the correlation of data: A guide to the transposition of streamflow	5-8
	<b>Table 5-3</b>	Curve numbers for events with annual peak discharge for Watershed 2 near Treynor, Iowa	5-11

---

<b>Figures</b>	<b>Figure 5-1</b>	Crest staff gage	5-3
	<b>Figure 5-2</b>	Sample of USGS surface water-supply paper showing recorded mean daily discharges	5-4
	<b>Figure 5-3</b>	Sample of USGS surface water-supply paper summarizing discharge records	5-5
	<b>Figure 5-4</b>	Two methods of plotting daily flow records	5-6
	<b>Figure 5-5</b>	Solution of runoff equation	5-9
	<b>Figure 5-6</b>	Rainfall versus direct runoff plotted from an experimental ARS watershed in Treynor, Iowa	5-12
<b>Examples</b>	<b>Example 5-1</b>	Total runoff for annual flood	5-6
	<b>Example 5-2</b>	Simple method to determine the direct runoff in inches for the annual flood of example 5-1	5-7
	<b>Example 5-3</b>	Determining runoff of gaged and ungaged watersheds that are alike in all respects	5-8
	<b>Example 5-4</b>	Classical graphical approach to establish runoff curve numbers	5-10
	<b>Example 5-5</b>	Statistical approach to establish runoff curve numbers	5-13

---

### 630.0500 Introduction

Streamflow data collected by various agencies describe the flow characteristics of a stream at a given point. Normally, data are collected by using a measuring device commonly called a stream gage.

Streamflow data are used to indicate the present hydrologic conditions of a watershed and to check methods for estimating present and future conditions. Specific uses presented in part 630 are for determining hydrologic soil-cover complex numbers (chapter 9), frequency analysis (chapter 18), determining water yields (chapter 20), and designing floodwater retarding structures (chapter 21). This chapter describes ways to use this information to determine runoff from a specific event, how to use this information with rainfall data to estimate the watershed runoff curve number, and how to use the data to determine volume-duration-probability relationships.

---

### 630.0501 Sources

Published streamflow data for the United States are available from many sources. The main sources are:

**U.S. Geological Survey (USGS, Department of Interior)**—Water Supply Papers (WSP) and other publications issued regularly contain records collected from continuously gaged streamflow stations and other crest stage and low flow data. USGS is the major source of streamflow data for the United States. Their publications are listed in Publications of the Geological Survey, which is issued in cumulative editions; yearly and monthly supplements are also issued. Complete files of WSP's are in USGS district offices. Some of the basic stream data are available on the USGS home page.

Descriptions of streamflow methods of gaging and other facts about USGS gaging practices are given in Measurement and Computation of Streamflow, Volume 1: Measurement of Stage and Discharge, and Volume 2: Computation of Discharge (USGS 1982).

**U.S. Bureau of Reclamation (BOR, Department of Interior)**—This agency gages and publishes streamflow data at irregular intervals in technical journals and professional papers.

**U.S. Forest Service (FS, Department of Agriculture)**—Streamflow data are published at irregular intervals in technical bulletins and professional papers.

**Agricultural Research Service (ARS, Department of Agriculture)**—ARS routinely publishes compilations of small watershed data. The most recent is Hydrologic Data for Experimental Agricultural Watersheds in the United States, 1978-79 (USDA, ARS 1989). This series is in 22 volumes. ARS also maintains REPHLEX, which is an online data base consisting of breakpoint rainfall-runoff data from ARS experimental watersheds. For information on this resource, contact the Water Data Center, ARS Hydrology Lab, Beltsville, Maryland. ARS practices are described in Field Manual Handbook 224 (USDA, ARS 1979).

**Corps of Engineers (COE, Department of Defense)**—COE obtains gage data and publishes streamflow data at irregular intervals in technical journals and professional papers. Most of the data appears in USGS publications.

**Natural Resources Conservation Service (NRCS, Department of Agriculture)**—NRCS gages and publishes streamflow data at irregular intervals in technical journals and professional papers. NRCS and the National Oceanographic and Atmospheric Administration's National Weather Service (NWS) jointly analyze snow and precipitation data in the Snow Survey Program. The data are used to forecast seasonal runoff in the western United States, which depends on snowmelt for about 75 percent of its water supply. The NRCS National Weather and Climate Center (NWCC) in Portland, Oregon, archives snow course, precipitation, streamflow, reservoir, and temperature data for states. The data, which includes many USGS gage sites, is accessible electronically.

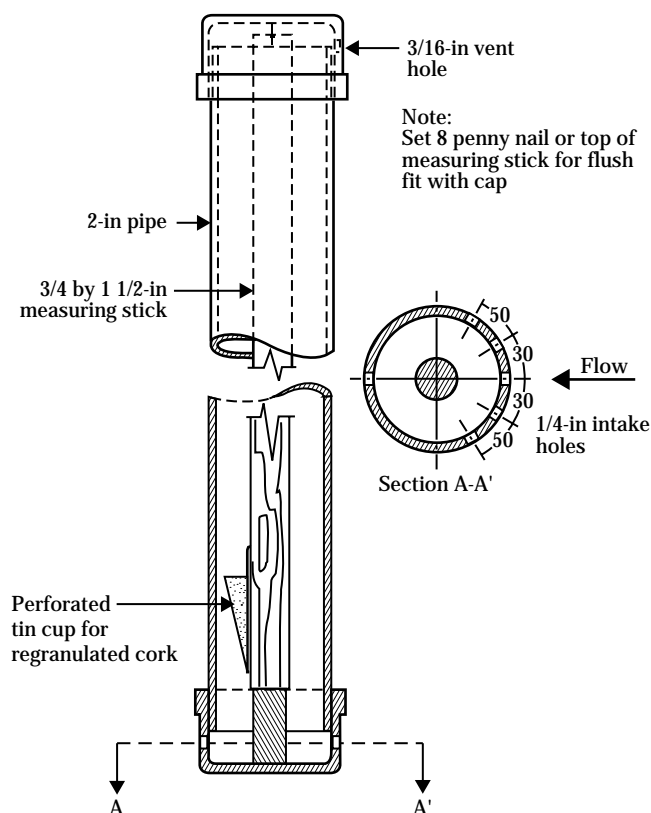
## 630.0502 Installation and operation of streamflow stations

NRCS cooperates with the USGS in the installation and operation of streamflow stations needed by NRCS. This cooperation is on a formal administrative basis, and the Engineering Division can advise on the administrative procedure (National Engineering Manual, Section 530.02).

### (a) Temporary streamflow station installations

Sometimes streamflow information is needed for a brief period on a small stream, irrigation ditch, gully, or reservoir, and the circumstances do not justify the installation of a continuous recorder. If the flow to be measured is small, measuring devices described in NEH-15, Chapter 9, Measurement of Irrigation Water, can be used. If only the maximum stage or peak rate of flow is needed, a crest staff gage can be used at a culvert or other existing structure. Figure 5-1 shows a typical inexpensive staff gage. The pipe of the gage contains a loose material (usually powdered cork) that floats and leaves a high-water mark or maximum stage. The stage is used with a rating curve (chapter 14) to estimate the peak rate of flow.

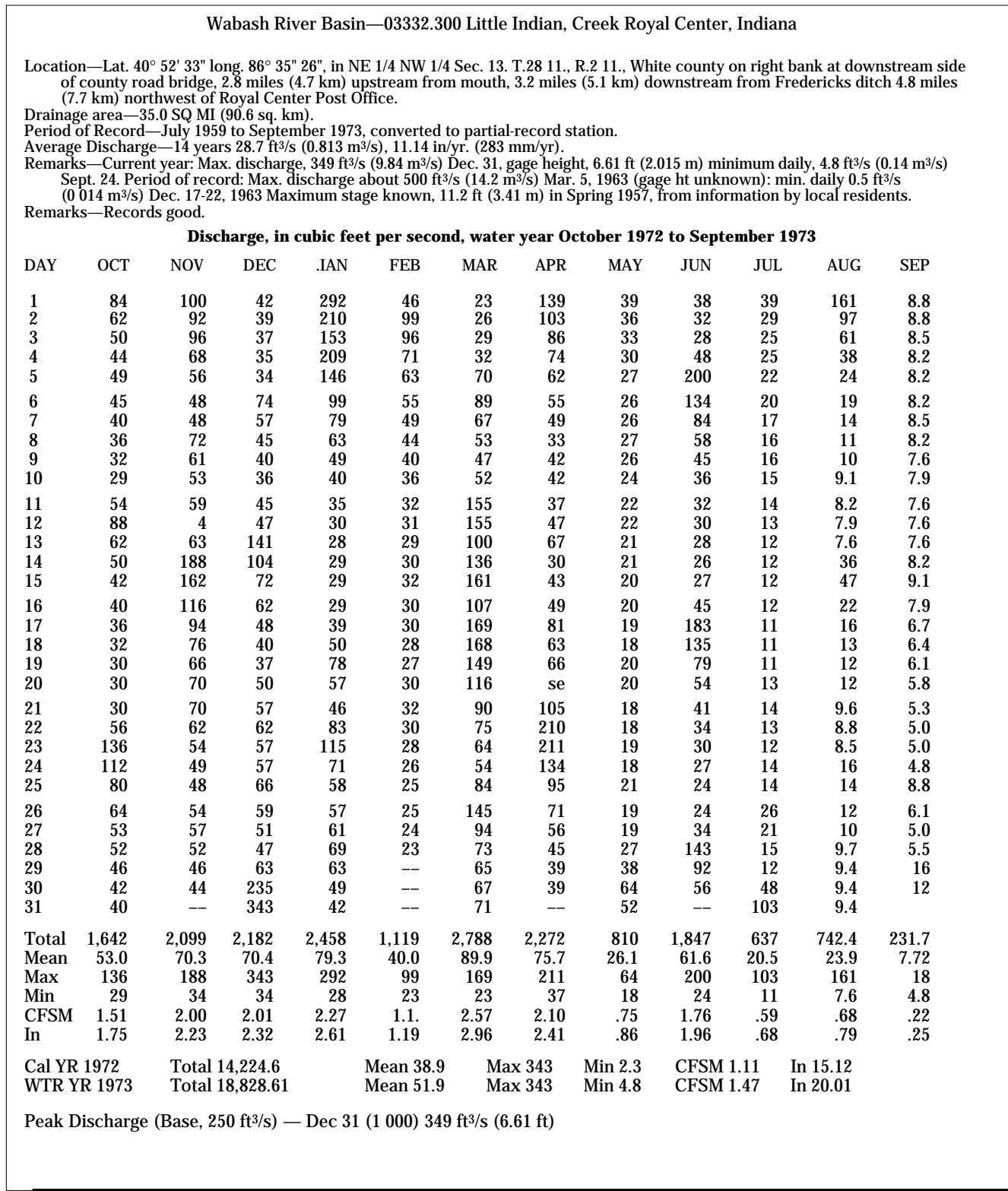


**Figure 5-1** Crest staff gage (USGS 1968, p.27)

## 630.0503 Streamflow data uses

### (a) Mean daily discharges

Records of mean daily discharges are generally published in the form shown in figure 5-2, a typical page from a water supply paper (WSP). Each state publishes an annual summary of the daily flows for each USGS station that contains continuous flow and stage data. Summaries of discharge records appear in various forms; a typical page from a WSP containing summaries is shown in figure 5-3. Summaries containing daily flow records were published cumulatively by USGS for 5-year increments until 1970. Figure 5-3 shows a page from an older WSP containing the summaries of all records for 1951 through 1960. Such older summaries covering longer periods do not have the daily flow records.

**Figure 5-2** Sample of USGS surface water-supply paper showing recorded mean daily discharges (USGS 1974)

**Figure 5-3** Sample of USGS surface water-supply paper summarizing discharge records (USGS 1964)

Nueces River Basin—2080 Atascosa River at Witsett, TX													
Location—Lat. 28°37'20" long. 98°17'05", on right bank 1,400 feet upstream from bridge on Farm Road 99, 0.9 mile west of Whitsett, Live Oak County, and 4 miles downstream from LaParita Creek.													
Drainage area—1,171 mi <sup>2</sup> .													
Records available—September 1924 to May 1926, May 1932 to September 1960.													
Gage—Water-stage recorder and artificial control. Datum of gage is 159.04 feet above mean sea level, datum of 1929. Prior to May 8, 1926, chain gage at bridge 1,600 feet downstream at datu 1.38 feet higher.													
Average discharge—29 years (1924-25, 1932-60), 135 ft <sup>3</sup> /s (97,740 acre-foot per year).													
Extremes—1924-26, 1932-60: Maximum discharge, 39,300 ft <sup>3</sup> /s July 7, 1942 (gage height, 38.3 feet from floodmark), from rating curve extended above 12,000 ft <sup>3</sup> /s on basis of slope-area measurement at gage height 38.0 feet; no flow at times. Maximum stage since at least 1881, about 41 feet in September 1919.													
Remarks—Considerable losses of floodflows into various permeable formations occur upstream from station. June 1951 to May 1958 a considerable part of low flow resulted from flow of several artesian wells near Campbellton, which were drilled by the Lower Nueces River Water Supply District and turned into river to supplement the supply for city of Corpus Christi. Small diversions above station.													
Monthly and yearly mean discharge, in cubic feet per second													
Water year	Oct	Nov	Dec	Jan	Feb	Mar	Apr	May	Jun	Jul	Aug	Sep	The year
1951	0.47	0.58	2.70	4.88	6.39	10.0	6.98	188	239	1.60	6.49	445	75.5
1952	20.0	20.7	13.9	17.5	48.5	14.9	65.4	39.2	6.76	114	6.74	246	50.7
1953	7.58	16.4	24.6	22.5	17.2	17.4	59.4	542	30.3	32.1	50.4	591	118
1954	76.3	13.9	10.0	9.97	15.6	15.2	62.3	43.8	39.8	7.59	0	3.29	24.8
1955	21.6	27.2	9.27	19.2	128	16.2	12.2	130	60.6	19.2	39.4	19.5	41.3
1956	378	5.21	11.7	11.6	11.3	10.6	31.9	62.8	21.6	14.5	68.0	177	35.5
1957	204	6.86	58.7	14.6	18.6	108	1,208	1,365	321	13.7	8.91	703	336
1958	10	241	23.4	940	1,499	64.7	30.7	208	23.8	4,734	3.09	118	267
1959	386	2,863	87.8	28.8	37.2	19.7	17.1	83.5	24.0	8.55	2.77	7.29	82.8
1960	200	31.2	1,109	16.7	17.2	31.5	22.1	10.1	201	142	135	14.2	69.7
Monthly and yearly discharge, in acre-feet													
1951	29	35	166	300	355	615	416	11,550	14,210	98	399	26,460	54,630
1952	1,230	1,230	852	1,080	2,790	915	3,890	2,140	402	7,000	415	14,610	36,820
1953	466	974	1,510	1,381	956	4,071	3,540	33,350	1,800	1,970	3,100	35,170	85,290
1954	4,690	828	617	613	865	936	3,710	2,700	2,370	467	0	196	17,990
1955	1,330	1,620	570	1,180	4,080	996	725	8,000	3,610	1,180	2,420	1,160	29,870
1956	48	310	721	716	649	652	1,900	3,860	1,290	889	4,180	10,530	25,740
1957	12,560	408	3,610	900	1,040	6,610	71,870	83,900	19,080	845	548	41,830	243,200
1958	6,170	14,330	1,440	57,800	83,230	3,980	1,830	12,770	1,410	2,920	190	7,010	193,100
1959	23,750	17,040	5,400	1,770	2,060	1,210	1,020	5,130	1,430	526	171	434	59,940
1960	12,300	1,860	732	1,030	990	1,940	1,620	619	11,970	5,710	8,330	844	50,640
Yearly discharge, in cubic feet per second													
Year	WSP	-----Water year ending September 30-----						-----Calendar year-----					
		Momentary maximum		Minimum		Mean		Acre-feet		Mean		Acre-feet	
		Discharge	Date	day									
1950	--	--	--	--	--	--	--	--	--	40.1	--	29,040	--
1951	1212	6,060	Sep 14, 1951	0.2	75.5	54,630	79.7	57,720					
1952	1242	4,000	Sep 10, 1952	.6	50.7	36,820	50.2	36,460					
1953	1282	6,550	Sep 5, 1953	2.6	118	85,290	122	88,470					
1954	1342	1,050	Apr 9, 1954	0	24.8	17,990	21.2	15,380					
1955	1392	1,570	Feb 7 1955	.7	41.3	29,870	37.9	27,430					
1956	1442	2,960	Sep 3, 1956	0	35.5	25,740	56.8	41,240					
1957	1512	8,410	May 29, 1957	1.6	336	243,200	343	248,600					
1958	1562	17,500	Feb 23, 1958	1.3	267	193,100	300	217,300					
1959	1632	3,830	Oct 31, 1958	1.0	82.8	59,940	39.6	28,640					
1960	1712	3,210	Jun 27, 1960	.7	69.7	50,640	--	--					

When using daily flow records, plot the discharge against time using one of the two ways shown in figure 5-4. In figure 5-4a, the mean daily flows are plotted as point values at midday using a logarithmic scale for discharge and an arithmetic scale for time. In figure 5-4b, both scales are arithmetic. A plotting like figure 5-4a is used in studying low flows or recession curves, and one like figure 5-4b can be used in studying high flows, for showing discharges in their true proportions, or for determining runoff amounts by measurement of areas. If a watershed has a rainfall to runoff response of about 20 hours or more, mean daily amounts are suitable for plotting flood hydrographs because there is little chance that more than one peak occurs in any one day. Watersheds that have shorter response times have flows that vary more widely during a day, so a hydrograph of mean daily records may conceal important fluctuations. A continuous record of flow should be used instead.

An important use of mean daily flows is in computing storm runoff amounts including baseflow (example 5-1) or excluding it (example 5-2).

#### Example 5-1 Total runoff for annual flood

Use data in figure 5-2 to determine total runoff (including baseflow) for the annual flood.

##### Determine:

Annual flood and largest peak rate in the year.

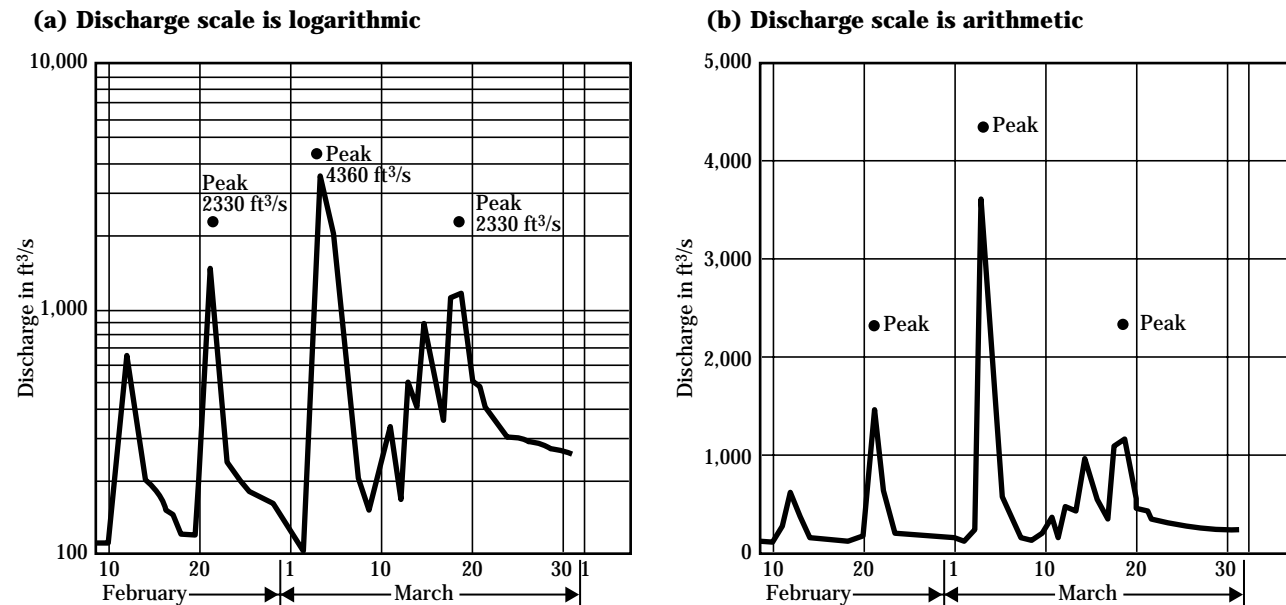
##### Solution:

In figure 5-2 under Extremes, maximum discharge is 349 ft<sup>3</sup>/s (9.88 cms) on December 31. Find the low point of mean daily discharge occurring before the rise of the annual flood. This point occurs on December 28 (table 5-1).

Find the date on the receding side of the flood when the flow is about equal to the low point of December 28. This occurs on January 9. The flows between January 9 and January 14 are considered part of the normal river flow, not part of the flood flow.

Add the mean daily discharges for the flood period from December 29 through January 9 (the starred discharges in table 5-1). The sum, which is the total runoff, is 1,941 ft<sup>3</sup>/s-day.

Figure 5-4 Two methods of plotting daily flow records



Runoff in cubic feet per second per day (ft<sup>3</sup>/s/d) can be converted to other units using appropriate conversion factors (a table of factors follows chapter 22). For instance, to convert the result in example 5-1 to inches, use the conversion factor 0.03719, the sum of step 4, and the watershed drainage area in square miles (from fig. 5-2):

$$\frac{0.03719(1941)\text{ft}^3/\text{s} - \text{days}}{35\text{mi}^2} = 2.0625\text{ in}$$

Round to 2.1 inches.

If the flow on the receding side does not come down far enough, the usual practice is to determine a standard recession curve using well-defined recessions of several floods, fit this standard curve to the appropriate part of the plotted record, and estimate the mean daily flows as far down as necessary.

**Table 5-1** Mean daily discharges, annual flood period (excerpt from fig. 5-2)

Date	Mean daily discharge (ft <sup>3</sup> /s)	Remarks
Dec. 26	59	Flow from previous rise
27	51	Flow from previous rise
28	47	Low point of flow
29	*63	Rise of annual flow begins
30	*235	Rise of annual flood continues
31	*343	Date of peak rate
Jan. 1	*292	Flood receding
2	*210	Flood receding
3	*153	Flood receding
4	*209	Flood receding
5	*146	Flood receding
6	*99	Flood receding
7	*79	Flood receding
8	*63	Flood receding
9	*49	Flood receding
10	40	End of flood period
11	35	Normal streamflow
12	30	Normal streamflow
13	28	Normal streamflow
14	29	New rise begins

\* Data used in example 5-1

If only the direct runoff (chapter 10) is needed, the baseflow can be removed by any one of several methods. A simple method assuming continuing constant baseflow may be accurate enough for many situations. This method is used in example 5-2.

**Example 5-2** Simple method to determine the direct runoff in inches for the annual flood of example 5-1

**Determine:**

Total runoff in cubic feet per second-day (ft<sup>3</sup>/s-day) (excluding baseflow) from example 5-1 data.

**Solution:**

Step 1—Determine the average baseflow for the flood period. This is an average of the flows on December 28 and January 9:

$$\frac{(47 + 49)}{2} = 48.0\text{ ft}^3/\text{s}$$

Step 2—Compute the volume of baseflow. Table 5-1 shows the flood period (starred discharges) to be 12 days; the volume of baseflow is:

$$12(48) = 576\text{ ft}^3/\text{s} - \text{day}$$

Step 3—Subtract total baseflow from total runoff to get total direct runoff:

$$1941 - 576 = 1365\text{ ft}^3/\text{s} - \text{day}$$

Step 4—Convert to inches. Use the conversion factor 0.03719 (from conversion table following chapter 22), the total direct runoff in cubic feet per second per day from step 3, and the watershed drainage area in square miles (from the source of data, table 5-2):

$$\frac{0.03719(1365)\text{ft}^3/\text{s} - \text{day}}{35\text{mi}^2} = 1.4504\text{ in}$$

Round to 1.45 inches.

(b) Transposition of streamflow records

Transposition of streamflow records is the use of records from a gaged watershed to represent the records of an ungaged watershed in the same climatic and physiographic region. Table 5–2 lists some of the data generally transposed and the factors affecting the correlations between data for the gaged and ungaged watersheds. The A means that a considerable amount of analysis may be required before a transposition is justified. Bulletin 17B, Guidelines for Determining Flood Flow Frequency, contains information and references on such topics as comparing similar watersheds and how to handle flooding caused by different type of events.

Data may be transposed with or without changes in magnitude depending on the kind and the parameters influencing them. Runoff volumes from individual storms, for instance, may be transposed without change in magnitude if the gaged and ungaged watersheds are alike in all respects. If the hydrologic soil-cover complexes (CN) differ though, it is necessary to use figure 5–5 as shown in example 5–3.

Transposition of flood dates and number of floods per year is described in chapter 18, and transposition of total and average annual runoff is described in chapter 20.

Example 5–3      Determining runoff of gaged and ungaged watersheds that are alike in all respects

**Given:**  
A gaged watershed with CN = 74 had a direct runoff of 1.6 inches.

**Determine:**  
The comparable runoff for a nearby ungaged watershed with CN = 83.

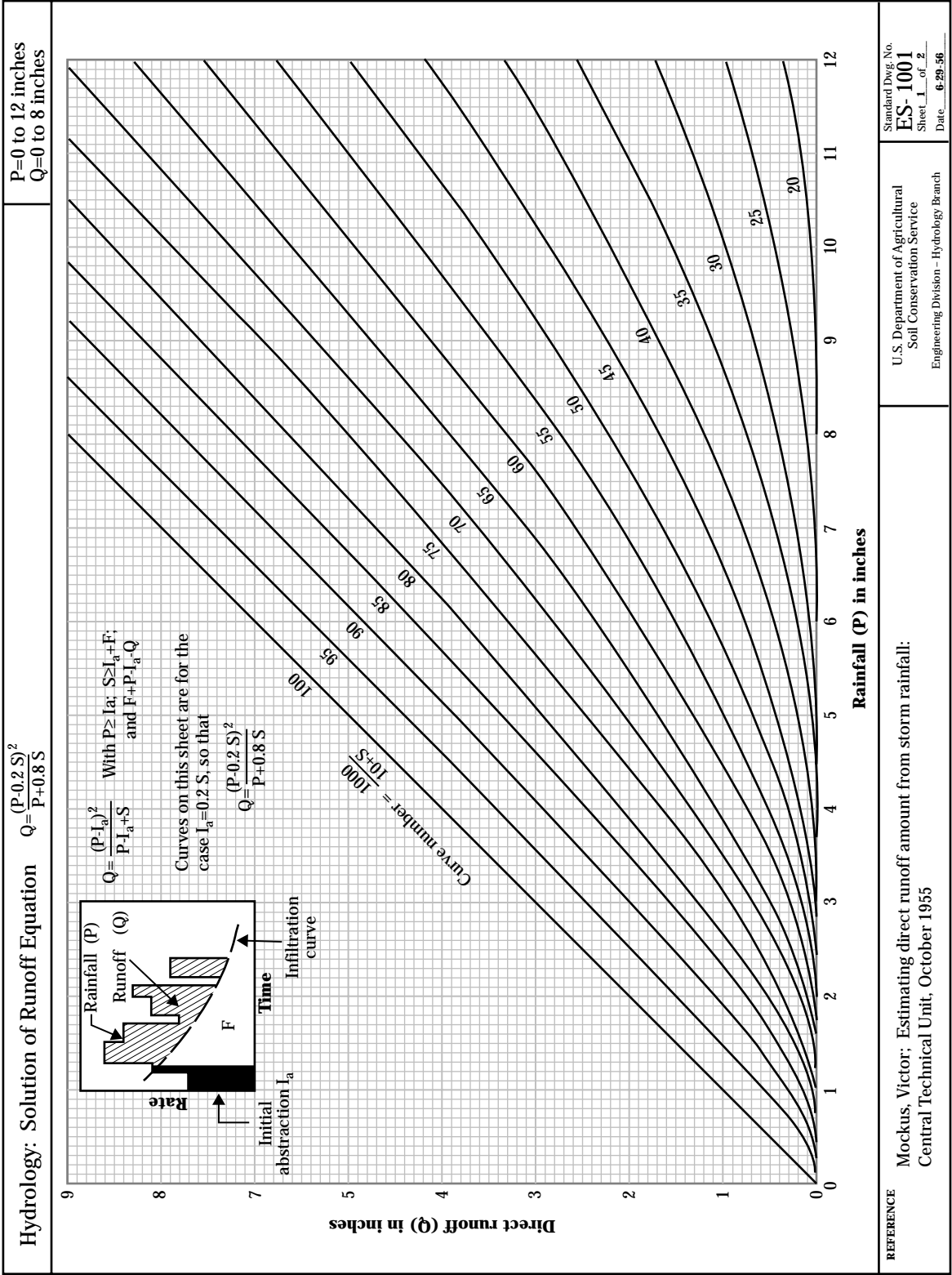
**Solution:**  
Enter figure 5–5 at runoff of 1.60 inches. Go across to CN 74 and then upward to CN 83. At the runoff scale read a runoff of 2.29 inches.

Table 5–2      Factors affecting the correlation of data: A guide to the transposition of streamflow

Data	Factors *				
	Large distance between watersheds	Large difference in sizes of watershed response lag	Runoff from small-area thunderstorm	Large difference in sizes of drainage area	Difference in hydrologic soil cover complexes
Flood dates	A	A	A	A	A
Number of floods per year	A	A	A	A	A
Individual flood, peak rate		A	A	A	A
Individual flood, volume			A	A	A
Total annual runoff			A	A	A
Average annual runoff				A	A

\*    A indicates adverse effect on the correlations. If no A the adverse effect is minor.

Figure 5-5 Solution of runoff equation



### (c) Volume-duration-probability analysis

Daily flow records are also used for volume-duration probability [VDP] analysis (USDA 1966 and HEC 1975). A probability distribution analysis of the annual series of maximum runoff volume for 1, 3, 7, 15, 30, 60, and 90 days is made (chapter 18). These values are then used for reservoir storage and spillway design (chapter 21). Low flow VDP analysis is made on minimum volumes over selected durations. These values are useful in water quality evaluations, e.g., for determining the probability that the concentration of a substance will be exceeded. They are also used to describe minimum flow for fisheries (USFWS 1976).

### (d) Flow duration curves

Daily flow records are also used to construct flow duration curves. These curves show the percentage of time during which specified flow rates are exceeded (HEC 1975). The flow duration curve is one method used to determine total sediment load from periodic samples (USDA 1983). It can also be used for determining loading of other impurities, such as total salts, and can be related to fishery values (USFWS 1976). Flow duration curves are sometimes plotted on probability paper. It should be noted that the value plotted is the percentage of time exceeded, and this should not be confused with probability of occurrence.

### (e) Determination of runoff curve numbers

Use of storm rainfall and associated streamflow data for annual floods is the best means of establishing runoff curve numbers, CN. Such curve numbers are superior to those established by other means, such as through the methods described in chapter 9. Two examples are given. The first describes the classical graphical approach, and the second describes a statistical approach.

#### **Example 5-4** Classical graphical approach to establish runoff curve numbers

**Given:**

Rainfall and runoff data of table 5-3.

**Determine:**

Curve number (CN) using the classic graphical method.

**Solution:**

Step 1—Make an electrostatic copy of figure 5-5.

Step 2—Plot the runoff against the rainfall on the graph as shown in figure 5-6.

Step 3—Determine the curve of figure 5-5 that divides the plotted points into two equal groups. That is the median curve number. It may be necessary to interpolate between curves, as was done in figure 5-6. The curve number for this watershed is 88.

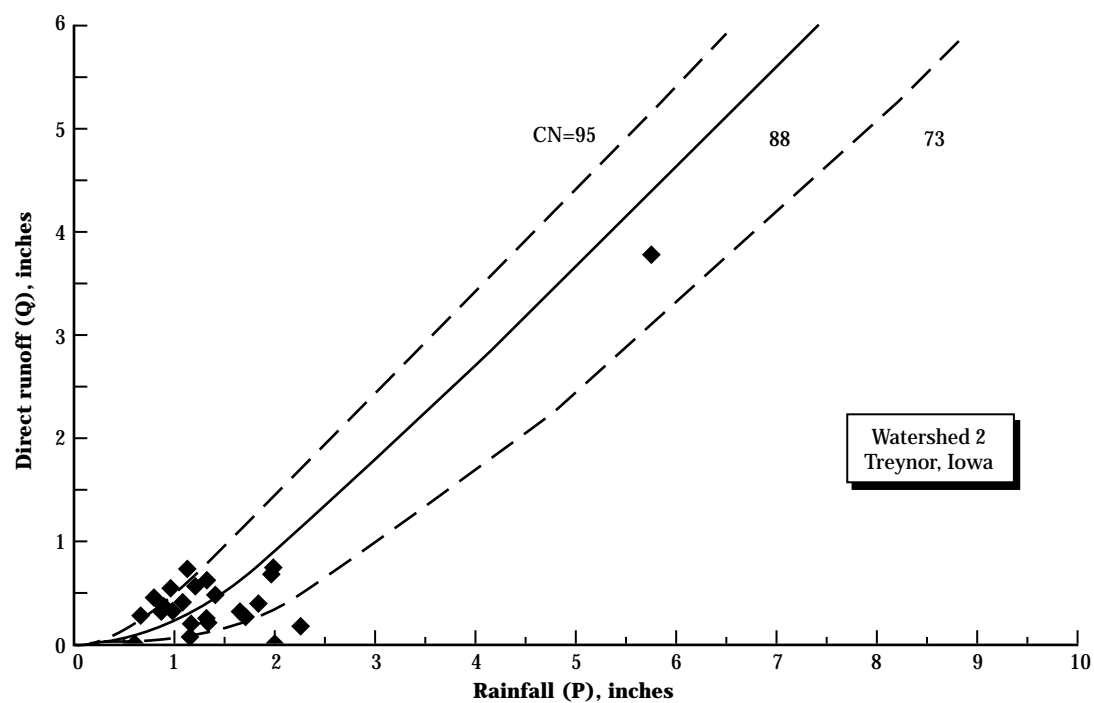
Figure 5-6 also shows bounding curves for the data. The curves were determined using the relationship given in table 5-3. Note that these curves generally mark the extremes of the data except for a few outliers.



**Table 5-3** Curve numbers for events with annual peak discharge for Watershed 2 near Treynor, Iowa

Watershed data: 82.8 acres of corn, using conventional tillage on contour, on Ida and Monona soils

Year	Month	Day	Rain amount (inch)	Runoff amount (inch)	Peak discharge (ft <sup>3</sup> /s)	S (inch)	Log(s)	CN	Rounded CN
1964	Jun	22	1.18	0.58	216.8	0.7826	-0.1065	92.7	93
1965	Jun	29	1.30	0.64	157.0	0.8601	-0.0665	92.1	92
1966	Jun	26	1.04	0.40	153.0	0.9538	-0.0205	91.3	91
1967	Jun	20	5.71	3.76	406.0	2.1386	0.3301	82.4	82
1968	Jun	13	0.97	0.28	94.0	1.1855	0.0739	89.4	89
1969	Aug	20	2.23	0.17	36.9	5.7593	0.7604	63.5	63
1970	Aug	2	1.92	0.70	282.4	1.8691	0.2716	84.3	84
1971	May	18	1.10	0.73	214.0	0.4038	-0.3938	96.1	96
1972	May	5	0.62	0.29	121.0	0.4426	-0.3540	95.8	96
1973	Sep	26	1.25	0.28	43.7	1.8674	0.2712	84.3	84
1974	Aug	17	1.12	0.10	23.5	2.7270	0.4357	78.6	79
1975	Aug	29	1.66	0.30	54.2	2.8590	0.4562	77.8	78
1976	Jul	17	0.57	0.02	4.2	1.8396	0.2647	84.5	84
1977	May	8	1.06	0.43	145.4	0.9129	-0.0396	91.6	92
1978	May	19	1.12	0.20	84.1	1.9431	0.2885	83.7	84
1979	Mar	18	0.93	0.54	17.2	0.4617	-0.3356	95.6	96
1980	Jun	15	0.83	0.34	207.0	0.7064	-0.1501	93.4	93
1981	Aug	1	1.63	0.33	104.0	2.6110	0.4168	79.3	79
1982	Jun	14	1.35	0.50	151.0	1.2917	0.1112	88.6	89
1983	Jun	13	1.78	0.41	104.0	2.6060	0.4160	79.3	79
1984	Jun	12	0.76	0.45	104.0	0.3627	-0.4405	96.5	97
1985	May	14	1.26	0.22	35.6	2.2159	0.3456	81.9	82
1986	Apr	27	1.94	0.75	191.0	1.7687	0.2477	85.0	85
1987	May	26	0.86	0.38	55.0	0.6643	-0.1776	93.8	94
1988	Jul	15	1.96	0.03	2.8	7.3724	0.8676	57.6	58

**Figure 5-6** Rainfall versus direct runoff plotted from an experimental ARS watershed in Treynor, Iowa

**Example 5-5** Statistical approach to establish runoff curve numbers**Given:** Rainfall and runoff data of table 5-3.**Determine:** CN by statistical methods.**Solution:**

In this approach, the scatter in the data apparent in figure 5-6 is assumed to be described by a lognormal distribution about the median. This approach has been explored by Hjelmfelt, et al. (1982), Hjelmfelt (1991), and Hauser and Jones (1991).

The curve number determined in example 5-4 was the curve number that divided the points into two equal groups. That is, it is the median curve number. This median value can also be determined using the following computations:

Step 1—Compute the potential maximum retention (S) for each of the annual storms of table 5-3 using:

$$S = 5 \left[ P + 2Q - \left( \Delta Q^2 + 5PQ \right)^{\frac{1}{2}} \right]$$

This equation is an algebraic rearrangement of the runoff equation of chapter 10.

Step 2—The logarithm of each S is taken. Base 10 was used for table 5-3; however, natural logarithms can also be used.

Step 3—The mean and standard deviation of the logarithms of S are determined. The mean of the transformed values, that is mean of log (S), is equivalent to the median of the raw values (Yuan 1933).

$$\log S = \text{mean}(\log S) = \frac{\sum(\log S)}{N}$$

$$\text{Std. Dev.}(\log S) = \sqrt{\frac{\sum[\log S - \text{mean}(\log S)]^2}{N - 1}}$$

For the data of table 5-3, the values computed are:

$$\text{mean log}(S) = 0.1389$$

$$\text{standard deviation log}(S) = 0.3452$$

Step 4—The mean of the logarithms of a lognormally distributed variable is the median of the original variable. Thus, the antilogarithm of the result of the standard deviation equation gives a statistical estimation of the median S. If base 10 logarithms are used:

$$\begin{aligned} \text{median } S &= 10^{\log} \\ &= 10^{0.1389} \\ &= 1.3769 \end{aligned}$$

**Example 5-5** Statistical approach to establish runoff curve numbers—Continued

Step 5—The curve number is then given by:

$$\begin{aligned} \text{CN} &= \frac{1000}{10 + S} \\ &= \frac{1000}{1 + 1.3769} \\ &= 87.9 \end{aligned}$$

Step 6—Curve numbers for 10% and 90% extremes of the distribution are given by

$$\log (S_{10}) = \text{mean} (\log S) + 1.282 \text{ std. dev. } (\log S)$$

$$\log (S_{90}) = \text{mean} (\log S) - 1.282 \text{ std. dev. } (\log S)$$

in which 1.282 and -1.282 are the appropriate percentiles of the normal distribution. For the data of table 5-3, the results are 73 and 95.

**Note:** These results are in good agreement with the extremes that were determined using the graphical method. Additional conformation that the 10 percent and 90 percent extremes agree with figure 5-5 is given by Hjelmfelt, et al. (1982) and Hjelmfelt (1991).

## 630.0504 References

- Hauser, V.L., O.R. Jones. 1991. Runoff curve numbers for the southern high plains. *Trans. Amer. Soc. Agricul. Engrs.*, vol. 3, no. 1. pp 142-148.
- Hjelmfelt, A.T. 1991. An investigation of the curve number procedure. *J. Hydraulic Eng., Amer. Soc. Civil Engrs.*, vol. 117, no. 6, pp 725-737.
- Hjelmfelt, A.T., L.A. Kramer, and R.E. Burwell. 1982. Curve numbers as random variables, *Rainfall-runoff relationship*. V.P. Singh, ed., Resources Publications, Littleton, CO, pp. 365-370.
- United States Army Corps of Engineers. 1975. Hydrologic engineering methods for water resource development, volume 3. Hydrologic Frequency Analysis, HEC, Davis, CA.
- United States Department of Agriculture, Agricultural Research Service. 1979. Field manual for research in agricultural hydrology. *Agricultural Handbook No. 224*.
- United States Department of Agriculture, Agricultural Research Service. 1989. Hydrologic data for experimental agricultural watersheds in the United States, 1978-79. *Misc. Pub. 1469*.
- United States Department of Agriculture, Forest Service. Stream-gaging stations for research on small watersheds. K.G. Reinhart and R.S. Pierce, *Agric. Handb.* 268.
- United States Department of Agriculture, Soil Conservation Service. 1966. Hydrology study—A multi-purpose program for selected cumulative probability, distribution analysis. W.H. Sammons, Natural Resources Conservation Service, SCS-TP-148, Washington, DC.
- United States Department of Agriculture, Soil Conservation Service. 1980. National engineering manual, part 630—Hydrology. Natural Resources Conservation Services, Washington, DC.
- United States Department of Agriculture, Soil Conservation Service. 1983. Transmission of sediment by water. *National Engineering Handbook, Section 3, Sedimentation, Chapter 4*, Natural Resources Conservation Service, Washington, DC.
- United States Fish and Wildlife Service. 1976. Methodologies for the determination of stream resource flow requirements: an assessment. C.B. Stalker and J.L. Arnette (ed.), Office of Biological Services, Utah State University, Logan, Utah.
- United States Geological Survey. 1964. Compilation of records of surface waters of the United States, October 1950 to September 1960, 11 Part 8. *Water Supply Paper 1732*, Western Gulf of Mexico Basin.
- United States Geological Survey. 1968. Techniques of water-resources investigations of the U.S. Geological Survey, chapter A7, stage measurement at gaging stations. *In* Book 3, *Application of Hydraulics*, T.J. Buchanan and W.P. Somers, U.S. Gov. Print. Of., Washington, DC.
- United States Geological Survey. 1979. Flow duration curves. *USGS Water Supply Paper 1542-A*, J.K. Searcy, Washington, DC.
- United States Geological Survey. 1981. WATSTORE users guide. *USGS Open File Report 79-1336*, Washington, DC.
- United States Geological Survey. 1982. Guidelines for determining flood flow frequency. Office of Water Data Coordination. *Bulletin 17B*.
- United States Geological Survey. 1982. Measurement and computation of streamflow, vol. 1: Measurement of stage and discharge, and vol. 2: Computation of discharge. S.E. Rantz and others, *USGS Water Supply Paper 2175*.
- United States Geological Survey. 1994. Water resources data for Indiana, 1973. *USGS Surface Water-Supply Papers*, prepared in cooperation with the state of Indiana and other agencies.